

1. Pojednostavni logičke operacije (ovakve zadatke imate u bilježnici):

a. $A \cdot 1 + \bar{A} \cdot 0 =$

b. $\bar{A} \cdot 1 + \bar{A}$

c. $A \cdot A + \bar{A} \cdot 1 =$

d. $A + \bar{A} + B =$

e. $A + B \cdot C + B \cdot \bar{C} + \bar{A} =$

f. $\overline{A + \bar{A}} =$

2. Pojednostavni logičke operacije - distributivnost (ovakve zadatke imate u bilježnici)

a. $A \cdot (\bar{A} + B) =$

b. $A \cdot (A + B) =$

c. $A + (\bar{A} \cdot B) =$

d. $B + A \cdot \bar{B} =$

e. $A \cdot B + A =$

f. $A \cdot B \cdot C + A \cdot B =$

g. $A \cdot \bar{B} + B \cdot (A + \bar{B}) =$

h. $A \cdot B + A \cdot \bar{B} + A \cdot C + C =$

3. Pojednostavni logičke operacije:

a. $\overline{\bar{A} \cdot (A + B)} =$

b. $\overline{\bar{A} \cdot B} + A =$

c. $\overline{A + B} \cdot A =$

d. $\overline{B \cdot (A + \bar{B})} =$

e. $\overline{\bar{A} \cdot (A \cdot B)} =$

f. $\overline{(\bar{A} + C)} \cdot \overline{(B + \bar{C})} =$

g. $A \cdot (A \cdot \bar{B} + \bar{A} \cdot B + \bar{B} \cdot C) =$

h. $\overline{A + (B \cdot C)} \cdot C =$

i. $A \cdot \overline{(A \cdot \bar{B} + \bar{A} \cdot B)} =$

j. $\overline{(A + B)} \cdot (A + \bar{B}) \cdot \overline{(\bar{A} + B)} =$

Rješenja:**1. Pojednostavni logičke operacije (ovakve zadatke imate u bilježnici):**

a. $A \cdot 1 + \bar{A} \cdot 0 = A + 0 = A$

b. $\bar{A} \cdot 1 + \bar{A} = \bar{A} + \bar{A} = \bar{A}$

c. $A \cdot A + \bar{A} \cdot 1 = A + \bar{A} = 1$

d. $A + \bar{A} + B = 1 + B = 1$

e. $\overline{A+B \cdot C + B \cdot \bar{C} + \bar{A}} = A + \bar{A} + B \cdot C + B \cdot \bar{C} = 1 + B \cdot C + B \cdot \bar{C} = 1$

f. $\overline{A + \bar{A}} = \bar{1} = 0$

2. Pojednostavni logičke operacije - distributivnost (ovakve zadatke imate u bilježnici)

a. $A \cdot (\bar{A} + B) = A \cdot \bar{A} + A \cdot B = 0 + A \cdot B = A \cdot B$

b. $A \cdot (A + B) = A \cdot A + A \cdot B = A + A \cdot B = A \cdot (1 + B) = A$

c. $A + (\bar{A} \cdot B) = (A + \bar{A}) \cdot (A + B) = 1 \cdot (A + B) = A + B$

d. $B + A \cdot \bar{B} = (B + A) \cdot (B + \bar{B}) = (B + A) \cdot 1 = B + A$

e. $A \cdot B + A = A \cdot (B + 1) = A \cdot 1 = A$

f. $A \cdot B \cdot C + A \cdot B = A \cdot B \cdot (C + 1) = A \cdot B$

i. $A \cdot \bar{B} + B \cdot (A + \bar{B}) = A \cdot \bar{B} + B \cdot A + B \cdot \bar{B} = A \cdot \bar{B} + B \cdot A + 0 = A \cdot \bar{B} + B \cdot A = A \cdot (B + \bar{B}) = A \cdot 1 = A$

j. $A \cdot B + A \cdot \bar{B} + A \cdot C + C = A \cdot (B + \bar{B} + C) + C = A \cdot (1 + C) + C = A \cdot 1 + C = A + C$

3. Pojednostavni logičke operacije: (složeniji zadatci)

a. $\overline{\bar{A} \cdot (A + B)} = \overline{\bar{A} \cdot A + \bar{A} \cdot B} = \overline{0 + \bar{A} \cdot B} = \overline{\bar{A} \cdot B} = \bar{\bar{A}} + \bar{B} = A + \bar{B}$

b. $\overline{\bar{A} \cdot B + A} = \overline{\bar{A} \cdot B \cdot \bar{A} + A} = \overline{A \cdot B \cdot \bar{A} + A} = \overline{A \cdot \bar{A} \cdot B + A} = \overline{0 \cdot B + A} = \overline{0 + A} = \bar{A}$

c. $\overline{\bar{A} + B \cdot A} = \overline{\bar{A} + B + \bar{A}} = \overline{A + B + \bar{A}} = \overline{A + \bar{A} + B} = \overline{1 + B} = \bar{1} = 0$

d. $\overline{B \cdot (A + \bar{B})} = \overline{B \cdot A + B \cdot \bar{B}} = \overline{B \cdot A + 0} = \overline{B \cdot A} = \bar{B} + \bar{A}$

e. $\overline{\bar{A} \cdot (A \cdot B)} = \bar{0} = 1$

f. $\overline{(\bar{A} + C) \cdot (B + \bar{C})} = \overline{(A \cdot \bar{C}) \cdot (\bar{B} \cdot \bar{C})} = \overline{(A \cdot \bar{C}) \cdot (\bar{B} \cdot C)} = \overline{A \cdot \bar{B} \cdot \bar{C} \cdot C} = \overline{A \cdot \bar{B} \cdot 0} = \bar{0} = 1$

g. $A \cdot (A \cdot \bar{B} + \bar{A} \cdot B + \bar{B} \cdot C) = A \cdot A \cdot \bar{B} + A \cdot \bar{A} \cdot B + A \cdot \bar{B} \cdot C =$

$A \cdot \bar{B} + 0 + A \cdot \bar{B} \cdot C = A \cdot \bar{B} + A \cdot \bar{B} \cdot C = A \cdot \bar{B} \cdot (1 + C) = A \cdot \bar{B}$

k. $\overline{A + (B \cdot C) \cdot C} = \overline{A + B \cdot C \cdot C} = \overline{A + (B + \bar{C}) \cdot C} = \overline{A + C \cdot (B + \bar{C})} =$

$\overline{A \cdot C \cdot B + A \cdot C \cdot \bar{C}} = \overline{A \cdot C \cdot B + 0} = \overline{A \cdot C \cdot B}$

$$\begin{aligned}
 \text{l. } & A \cdot (\overline{A \cdot \overline{B} + \overline{A} \cdot B}) = A \cdot (\overline{A \cdot \overline{B} \cdot \overline{\overline{A} \cdot B}}) = A \cdot (\overline{\overline{A} + \overline{B}}) \cdot (\overline{\overline{\overline{A} + \overline{B}}}) = (A \cdot \overline{A} + A \cdot B) \cdot (A + \overline{B}) = \\
 & A \cdot B \cdot (A + \overline{B}) = A \cdot B \cdot A + A \cdot B \cdot \overline{B} = A \cdot B + 0 = A \cdot B
 \end{aligned}$$

$$\begin{aligned}
 \text{m. } & (\overline{A + \overline{B}}) \cdot (A + \overline{B}) \cdot (\overline{\overline{A + \overline{B}}}) = \overline{A} \cdot \overline{B} \cdot (A + \overline{B}) \cdot \overline{\overline{\overline{A} \cdot \overline{B}}} = \overline{A} \cdot \overline{B} \cdot \overline{\overline{\overline{A} \cdot \overline{B}}} \cdot (A + \overline{B}) = \\
 & \overline{A} \cdot A \cdot \overline{B} \cdot \overline{B} \cdot (A + \overline{B}) = 0 \cdot (A + \overline{B}) = 0
 \end{aligned}$$